Two- and Multi-Party Protocols JASS 2005

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Why cryptographic protocols?

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- cryptography is concerned with secure communication
- various other tasks
- enable to solve many real-world problems electronically
- theoretical any given functionality can be performed with protocols

∇ Two- and Multi-Party Protocols – p.2/43



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But what's that! All printers in the department seem to malfunction. So Joe needs a way to electronically timestamp his work.















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- no privacy (transmission, database)
- no efficiency (huge database)
- errors may occure (transmission, database)
- third party may not be honest







We use one-way hashfunctions and digital signatures to enhance the protocol.



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- privacy (only hash is revealed)
- efficiency (no database is needed)
- no errors (examine signed hash immediately)
- remaining Problem: Joe and Anja might work together















This protocols makes it very hard for Joe to cheat.
Timestamping - Final Try (II)

This protocols makes it very hard for Joe to cheat.

- for selection: random-number-generator with hash of document as input
- choose k sufficiently high
- only a subset of k persons should suffice for a valid timestamp

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Mental Poker - Requirements

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- Joe generates 52 messages M_1, M_2, \ldots, M_{52}
- unique random string
- $E_J(M_i) := M_i$ encrypted with Joes public-key'
- $D_S(X) := X$ decrypted with Steves private-key'
- cryptographic algorithm commutative, i.e. $D_S(E_L(E_S(X))) = E_L(X)$



















Mental Poker - Discussion

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- additional cards
- everyone reveals his hand and keys after the game
- desired: only winner reveals his hand, but this is not secure
- implementation is not effective

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'Maybe next week I should try this with Lee from Tokyo?'













Bit Commitment - Discussion

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- random-bit string is important
- impossible to cheat
- several other protocols for this task
- e.g. involving one-way functions or pseudo-random-sequence generators

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Steve:'Ok, I will show you how.'









Steve explains following protocol, which uses a one-way function f. Steve chooses a random number r



'Your guess is right so its heads'



Coin Flipping - Discussion

∇ Two- and Multi-Party Protocols – p.18/43

Coin Flipping - Discussion

- security rests in one-way function
- least significant bit of f(x) and x must be uncorrelated
- use some other bit
- several other protocols exist

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Call me a.s.a.p.

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'I'll give you half the pages for half the price. You will get a good impression of my work and I get the money it is worth.

Anja:'Ok, but I want to choose the pages, so you don't send me the boring ones.'

Oblivious Transfer - Requirements

⊽ Two- and Multi-Party Protocols – p.20/43

Oblivious Transfer - Requirements

- Anja will receive only half of the pages
- Joe will not know which pages Anja receives
- Here: Joe sends Anja one of two messages M_1, M_2
- Joe generates two public-key/private-key pairs K_1, K_2
- Anja chooses a key K_A in a symmetric algorithm (e.g. DES)









Oblivious Transfer - Discussion

Oblivious Transfer - Discussion

- one message is gibberish
- other is plain
- Joe may encrypt two identical messages
- reveal Joes private-key later
- protocol is strange but useful

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Since he is a computer crack he immediately accepts, when the clerk asks him to take part in an experiment with digital cash.

Reto the bank clerk first explains to Joe, what a blind signature is.

Blind Signatures - Requirements

∇ Two- and Multi-Party Protocols – p.24/43

Blind Signatures - Requirements

- Reto shall sign a document without knowing the content
- in real-life: envelope and carbon paper
- signature function S commutes with an encryption Ei.e. D(S(E(m)) = S(m)
- RSA and one-time pads









Blind Signature - Discussion

∇ Two- and Multi-Party Protocols – p.26/43

Blind Signature - Discussion

- when Joe decrypts he gets the signed message
- Reto can not know which document he signed
- Reto can even get the signed document
- Reto signs many documents
- 'Reto owes Joe \$ 1.000.000'

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Story - Part VII

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Digital Cash - Requirements

∇ Two- and Multi-Party Protocols – p.28/43

Digital Cash - Requirements

- forgery has to be prevented or detected
- duplication has to be prevented or detected
- customers' anonymity has to be preserved
- no audit trails
- efficiency

Blind Signature enhanced

We want to prevent Joe from cheating.

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- present 100 documents to Reto
- Reto opens 99 documents at random
- all 99 documents should have the same content

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- Payment: verify signature
- Deposit: verify signature and then credit \$ 1000

DC Protocol # 1 - Discussion

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DC Protocol # 1 - Discussion

- anonymity
- no cheating
- double spending problem'

To solve the double spending problem we alter the protocol as follows.

random uniqueness string for each money order

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- Deposit: verify uniqueness string has not been used already

Protocol # 2 does prevent cheating but does not identify the cheater. So we will alter the protocol some more.

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 - uniqueness and identity string in the database then the merchant cheated

Money Order

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Money Order

before payment

Amount uniqeness string

Signature

Money Order



DCP # 4 Money Order Creation

We now want to discover who cheated, when the merchant is honest.

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- \bullet *n* pairs of identity bit strings generated as follows
- an identity string stating Joes name, address, etc.
- split this into two pieces using a 'secret splitting protocol'
- commit to each piece (bit-commitment)
- any pair reveals Joes identity when opened (e.g. I_{23_L} and I_{23_R} but not I_{23_L} and I_{42_R})

Money Order - After Withdrawal

⊽ Two- and Multi-Party Protocols – p.36/43

Money Order - After Withdrawal

after withdrawal



DCP # 4 Withdrawal and Payment

⊽ Two- and Multi-Party Protocols – p.37/43

DCP # 4 Withdrawal and Payment

- Withdrawal: Reto verifies that all 99 messages are well formed
 - amount
 - uniqueness string
 - all identity strings

DCP # 4 Withdrawal and Payment

- Withdrawal: Reto verifies that all 99 messages are well formed
 - amount
 - uniqueness string
 - all identity strings
- Payment: merchant will give Joe a random n-bit selector string b
- Joe will open either the left or right half, depending on b
- the random identity string is not used anymore

Money Order - identity strings
Money Order - identity strings

before payment



Money Order - identity strings



 $I_{n_L} = I_{n_R}$

Signature

Amount uniqeness string $I_{1_L} = I_{1_R}$ I_{2L} I_{2R} $I_{3L} = I_{3R}$ $I_{n_L} = I_{n_R}$ Signature

DCP # 4 - Deposit

⊽ Two- and Multi-Party Protocols – p.39/43

DCP # 4 - Deposit

- Deposit: Reto will check signature and uniqueness string
 - if uniqueness string is not used yet, record it and all the identity information
 - if the money is double spent, compare identity information
 - if they are identically the merchant has cheated
 - if not identity information is revealed

Digital Cash - Summary

Two- and Multi-Party Protocols – p.40/43

Digital Cash - Summary

- forgery is prevented by eBSP
- duplication is detected with uniqueness string
- customers' anonymity is preserved, as long as he does not cheat
- no audit trails exist, as long as the customer does not cheat
- efficiency

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If Joes proof of $P \neq NP$ really holds you may read in the next volume of 'Computer Science Weekly'

The End

That's it. (Just kidding)

The End

Thank you for your attention.